Volume Of Revolution - Disc Method

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Questions in past papers often come up combined with other topics.
Topic tags have been given for each question to enable you to know if you can do the question or whether you need to wait to cover the additional topic(s).

Scan the QR code(s) or click the link for instant detailed model solutions!

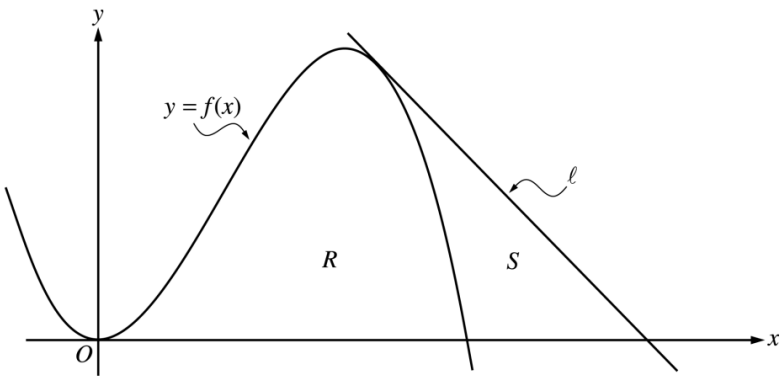
Question 1

Qualification: AP Calculus AB

Areas: Applications of Integration, Applications of Differentiation

Subtopics: Tangents To Curves, Integration - Area Under A Curve, Integration - Area Between Curves, Volume of Revolution – Disc Method

Paper: Part A-Calc / Series: 2003-Form-B / Difficulty: Hard / Question Number: 1



1. Let f be the function given by $f(x) = 4x^2 - x^3$, and let ℓ be the line $y = 18 - 3x$, where ℓ is tangent to the graph of f. Let R be the region bounded by the graph of f and the x-axis, and let S be the region bounded by the graph of f, the line ℓ, and the x-axis, as shown above.

   (a) Show that ℓ is tangent to the graph of $y = f(x)$ at the point $x = 3$.

   (b) Find the area of S.

   (c) Find the volume of the solid generated when R is revolved about the x-axis.

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Question 2

Qualification: AP Calculus AB

Areas: Applications of Integration

Subtopics: Integration - Area Under A Curve, Volume of Revolution – Disc Method, Volume of Revolution – Washer Method

Paper: Part A-Calc / Series: 2004-Form-B / Difficulty: Easy / Question Number: 1

1. Let R be the region enclosed by the graph of $y = \sqrt{x-1}$, the vertical line $x = 10$, and the x-axis.

   (a) Find the area of R.

   (b) Find the volume of the solid generated when R is revolved about the horizontal line $y = 3$.

   (c) Find the volume of the solid generated when R is revolved about the vertical line $x = 10$.

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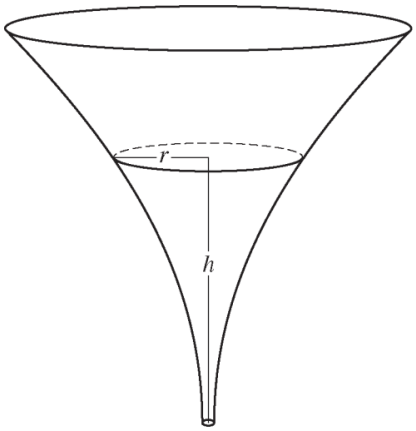
Question 3

Qualification: AP Calculus AB

Areas: Applications of Integration

Subtopics: Average Value of a Function, Volume of Revolution – Disc Method, Rates of Change (Instantaneous), Integration Technique – Standard Functions, Modelling Situations, Related Rates

Paper: Part B-Non-Calc / Series: 2016 / Difficulty: Medium / Question Number: 5



5. The inside of a funnel of height 10 inches has circular cross sections, as shown in the figure above. At height h, the radius of the funnel is given by $r = \frac{1}{20}\left(3 + h^2\right)$, where $0 \le h \le 10$. The units of r and h are inches.

   (a) Find the average value of the radius of the funnel.

   (b) Find the volume of the funnel.

   (c) The funnel contains liquid that is draining from the bottom. At the instant when the height of the liquid is $h = 3$ inches, the radius of the surface of the liquid is decreasing at a rate of $\frac{1}{5}$ inch per second. At this instant, what is the rate of change of the height of the liquid with respect to time?

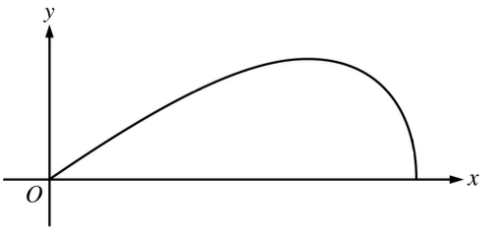
Question 4

Qualification: AP Calculus AB

Areas: Applications of Differentiation, Applications of Integration, Integration

Subtopics: Integration - Area Under A Curve, Integration Technique – Substitution, Local or Relative Minima and Maxima, Volume of Revolution – Disc Method

Paper: Part B-Non-Calc / Series: 2021 / Difficulty: Medium / Question Number: 3



3. A company designs spinning toys using the family of functions $y = cx\sqrt{4 - x^2}$, where c is a positive constant. The figure above shows the region in the first quadrant bounded by the x-axis and the graph of $y = cx\sqrt{4 - x^2}$, for some c. Each spinning toy is in the shape of the solid generated when such a region is revolved about the x-axis. Both x and y are measured in inches.

   (a) Find the area of the region in the first quadrant bounded by the x-axis and the graph of $y = cx\sqrt{4 - x^2}$ for $c = 6$.

   (b) It is known that, for $y = cx\sqrt{4 - x^2}$, $\frac{dy}{dx} = \frac{c\left(4 - 2x^2\right)}{\sqrt{4 - x^2}}$. For a particular spinning toy, the radius of the largest cross-sectional circular slice is 1.2 inches. What is the value of c for this spinning toy?

   (c) For another spinning toy, the volume is 2π cubic inches. What is the value of c for this spinning toy?